Back to Mathematical Foundations and Graphical Representations

1. Introduction

Our intellectual journey has traversed various terrains, from solid mathematical formulations to speculative idea sketches. This section aims to ground the discourse back to its mathematical roots, focusing on the graphing of superposition states.

2. Mathematical Formulation

The wavefunction for a quantum state in superposition with states tending to -1, 0, and +1 is given as follows:

$$|\Psi(\mathbf{x})\rangle = \alpha C + \beta U + \gamma(-1) + \delta 0 + \varepsilon(+1)$$

3. Graphical Representation

A plot can serve as a powerful tool for visualising complex quantum states. The graph below provides a visual representation of the superposition state, based on the mathematical formulation.

4. Python Code and Matplotlib

The graph was generated using Python and Matplotlib, illustrating how code can serve as an effective tool for scientific exploration.

5. Extended Mathematical and Python Code Exploration

Further mathematical intricacies can be explored by dissecting the superposition state into its individual components. Each component can be studied to understand its contribution to the overall wavefunction. Below are the individual components:

- αC
- βU
- γ(-1)
- - δ0
- -ε(+1)

The Python code has been extended to include multiple plots that showcase the contributions of these individual states to the superposition. This serves as a deeper dive into the mathematical intricacies of the quantum state in question.

6. Graphing Dynamic Systems in 4D (X, Y, Z, Time)

Extending our mathematical exploration, consider a dynamic system that evolves in a fourdimensional space represented by x, y, z coordinates along with time as a variable. In such a system, an observer with a static view of x, y, and z would perceive the system as a constantly evolving entity.

6.1 Mathematical Formulation

The mathematical representation of such a dynamic system could be a function (f(t)) that maps time (t) to a point in the 3D space (x, y, z). For instance, a function of the form:

(f(t) = (x(t), y(t), z(t)))

6.2 Python Code and Visual Representation

Python code utilizing libraries such as Matplotlib can be employed to visualize this dynamic system. A 3D plot or even an animation can serve to capture the system's evolution over time.

7. Topological Space with Interlaced Planar Topography

This section explores a conceptual model of a topological space with interlaced planar topography. The x, y, and z axes represent a continuum ranging from 'no beginning' to '13.8 billion years' to 'no end'. Interlaced planes within this topological space serve as potential fields for particles or objects. These fields, conceptualised as contours or isothermic patterns, peak at the location of particles.

7.1 Visual Representation

A 3D plot was generated to provide a visual representation of this complex topological space. The semi-transparent planes symbolize different levels of interlaced topography, and the red points represent particles within these fields.

Interlaced Planar Topography with Particles



8. Refined Topological Space with Light Properties

This section explores a refined conceptual model of a topological space that incorporates properties of light. The x-axis now represents frequencies of visible light in Hz, ranging from (4 times 10^{14}) Hz to (8 times 10^{14}) Hz. The y-axis corresponds to wavelengths in meters, calculated from the frequencies using the speed of light. The z-axis continues to represent the conceptual range from 'no beginning' to '13.8 billion years' to 'no end'. This integration adds a layer of physical realism to the existing topological model.

8.1 Visual Representation

The 3D plot below provides a visual representation of this refined topological space. The semi-transparent planes have been color-mapped to represent different levels within this conceptual range, and the red points symbolize particles within these fields.

Refined Topological Space with Light Properties



9. Topological Space with Celestial Objects

This section delves into a further refinement of the topological space, incorporating celestial objects to add another layer of complexity. The model now includes the Earth/Sun system, the 100 closest stars, the 100 brightest stars, and the 100 closest exoplanet stars. Each set of celestial objects is represented by a different colour in the 3D plot.

9.1 Visual Representation

The 3D plot below provides a visual representation of this further refined topological space. The axes have been augmented to include Declination (Dec) for x and Right Ascension (RA) for y, along with distance for the z-axis. This integration allows for a more comprehensive understanding of the topological space.



10. Topological Space with Uniform Scales

This section introduces a critical update to the topological space model by standardising all axes to a uniform scale of -1, 0, and +1. This adjustment allows for a more symmetrical representation of the conceptual space, further generalising its applicability. Each axis now serves as a conceptual range, akin to Declination (Dec), Right Ascension (RA), and distance in astronomical terms.

10.1 Visual Representation

The 3D plot below offers a visual representation of this uniformly scaled topological space. All axes are scaled from -1 to +1, providing a symmetrical framework for representing the conceptual space. This modification aims to achieve a more comprehensive and universally applicable topological model.



11. Topological Space with Time-Representing Planes

This section introduces yet another layer of complexity by incorporating time-representing planes into the topological space model. These planes serve as representations of different 'times' or 'epochs' within the existing z-structure. They are color-mapped based on their frequency, with blue representing the highest frequency, followed by green and red.

11.1 Visual Representation

The 3D plot below offers a visual representation of this advanced topological space. The semi-transparent planes symbolize different 'times' or 'epochs' within the conceptual range. Each is distinguished by a unique colour—blue for -1, green for 0, and red for +1—based on its frequency. This addition enriches the existing topological model by adding a temporal dimension.



12. Topological Space with Specified Coordinates for Time-Representing Planes

In this section, the time-representing planes are given specific coordinates within the topological space model. Blue serves as the background to the x & y axes, green marks the intersection of 0 on the z-axis with the xy-plane, and red is positioned at z + 1 in correspondence with the xy-plane.

12.1 Visual Representation

The 3D plot below visually depicts this precise placement of time-representing planes within the topological space. Each plane is color-coded—blue, green, and red—to signify its specific coordinate within this framework. Such specificity adds another layer of detail to our evolving topological model.



Topological Space with Specified Coordinates for Time-Representing Planes

13. Topological Space with Extended Spectrum Time-Representing Planes

This section explores further refinements to the topological space model by incorporating an extended spectrum of time-representing planes. The model now includes black and white planes, as well as amber spectrumed sublayers, denoted by shades of orange, between blue, green, and red.

13.1 Visual Representation

The 3D plot below visualises this intricately refined topological space. The variety of coloured planes represent different 'times' or 'epochs' within the conceptual range. The extended spectrum adds a level of granularity to the model, capturing a wider range of conceptual 'times'.



Topological Space with Extended Spectrum Time-Representing Planes

14. Topological Space with Only the Green Plane

This section explores a stripped-down version of the topological space model, wherein only the green plane representing 'z=0' is retained. This simplification serves as a focal point for further exploration.

14.1 Visual Representation

The 3D plot below provides a visual representation of this simplified topological space. Here, only the green plane is retained, representing 'z=0' within the conceptual range. This construct offers a minimalist perspective, laying the foundation for subsequent refinements.



15. Topological Space with Redefined Superposition

In this intriguing development, the superposition is redefined within the topological space model. The following redefinitions are applied: '-1' becomes '0', '0' becomes '1', and '1' becomes '-1'. This transformation alters the mathematical relationships within the model, offering new avenues for exploration.

15.1 Mathematical Description

Let ($z_{ ext{old}}$) represent the original z-coordinates, and ($z_{ ext{new}}$) the new z-coordinates. The transformation can be described by the following function: [$z_{ ext{new}}(z_{ ext{old}}) = -z_{ ext{old}} + 1$]

15.2 Visual Representation

The 3D plot below visualises this topological space with redefined superposition. The green plane, previously at 'z=0', is now at 'z=1', in accordance with the new mathematical relationships. This redefinition adds complexity and opens the door to further mathematical and conceptual inquiries.



16. Base Model: Topological Space with Green Plane

This section revisits the simplified topological space model with only the green plane at 'z=0'. This construct serves as the base model for subsequent developments and refinements.

16.1 Visual Representation

The 3D plot below reiterates this as the base model for further explorations. The green plane, representing 'z=0', serves as a stable reference point for adding complexities.



Base Model: Topological Space with Green Plane

17. Topological Space with Extended Fields

This section introduces an extension to the base model by adding new fields at 'z=-3' and 'z=3'. These additional planes serve as markers for further gradations within the topological space. The concept introduces a wave-like transition between these fields.

17.1 Mathematical Description

ext{extended}}) represent the new extended z-coordinates. The transition Let (z_{f}) from one field to another is wave-like and can be modeled as follows:

ext{extended}}(z) = sin(z)]This sine function serves as a mathematical [z { representation of the wave-like transition.

17.2 Visual Representation

The 3D plot below visualises this topological space with extended fields. The added fields at 'z=-3' and 'z=3' expand the conceptual range and serve as markers for gradations. This structure adds complexity and introduces wave-like transitions.



18. Topological Space with Gradient Planes

This section adds further nuance to the extended fields model by incorporating gradient planes at each whole number along the z-axis. The gradients oscillate between blue, green, and red, providing a visual mechanism to comprehend the gradational nature of the conceptual space.

18.1 Mathematical Description

Let (z_{ ext{gradient}}) represent the new gradient z-coordinates. The oscillation of colors between these gradient planes can be modeled as follows:

 $[z_{\{ c_{z_{\{ cos(z) \}}(z) = cos(z) \}}]$ This cosine function serves as a mathematical representation of the color oscillation.

18.2 Visual Representation

The 3D plot below visualises this topological space with gradient planes. The inclusion of these gradient planes adds an extra layer of complexity, enabling a more nuanced understanding of the topological space.



19. Topological Space with Messier Objects and Closest Galaxies

This section refines the existing model by incorporating messier objects and closest galaxies. These additions provide a more intricate landscape within the topological space, adding another layer of complexity and nuance.

19.1 Mathematical Description

Let (M) represent the set of messier objects and (G) represent the set of closest galaxies. Each element in (M) and (G) is defined as a triplet ((x, y, z)) representing its position in the topological space.

19.2 Visual Representation

The 3D plot below visualises this refined topological space with messier objects and closest galaxies. Purple triangles represent messier objects, and orange squares represent the closest galaxies. This inclusion brings an additional layer of intricacy to the model.



Topological Space with Gradient Planes and Messier Objects & Closest Galaxies

20. Refined Topological Space with a Single Plane at z=0

This section further simplifies the existing model by removing all gradient planes except for a single light-colored plane at z=0. This singular plane serves as a focal point within the topological space, streamlining the model while retaining its complexity.

20.1 Mathematical Description

The model now includes a single plane at (z = 0). Mathematically, this plane can be represented as a set of points ((x, y, z)) where (z = 0).

20.2 Visual Representation

The 3D plot below visualises this refined topological space with a single plane at z=0. The light-colored plane at z=0 serves as a focal point, providing a streamlined yet complex landscape.



Refined Topological Space with a Single Plane at z=0

21. Refined Topological Space with Frequency and Wavelength

This section further refines the existing model by adding the dimensions of frequency and wavelength to the x and y axes respectively. These new dimensions introduce another layer of complexity, allowing for a richer understanding of the topological space.

21.1 Mathematical Description

Let (lambda) represent wavelength along the x-axis and (f) represent frequency along the y-axis. Each point in this refined model can now be represented as a four-tuple ((lambda, f, x, y, z)), where (x, y, z) are the original coordinates.

21.2 Visual Representation

The 3D plot below visualises this refined topological space with the added dimensions of frequency and wavelength. Purple triangles represent points plotted with these new dimensions, thereby enriching the topological model.



Refined Topological Space with Frequency and Wavelength

22. Topological Space Shifted Back by 100,000 Time Units

This section introduces the concept of looking back in time to visualize the state of the topological space 100,000 time units ago. For this simulation, it's assumed that every celestial object moves at a constant velocity in a random direction over time.

22.1 Mathematical Description

Let (x', y', z') represent the shifted positions of the celestial objects. These are calculated using the formula:

(x' = x - v_x cdot t)
(y' = y - v_y cdot t)
(z' = z - v_z cdot t)
where (v_x, v_y, v_z) are the velocities along the x, y, and z axes respectively, and (t =
100,000) is the time shifted back.

22.2 Visual Representation

The 3D plot below visualises the topological space as it would have appeared 100,000 time units ago. Purple triangles represent the shifted positions of the Messier objects.



Topological Space Shifted Back by 100000 Time Units

23. Particle Cloud Description of Local Vision

This section explores the notion of 'local vision' within the topological space, representing celestial objects as elements of a particle cloud. This concept combines the current and past positions of celestial objects to create a fuller, dynamic view.

23.1 Mathematical Description

In this model, the celestial objects are represented as points in a high-dimensional space, forming what can be described as a particle cloud. This allows for a more nuanced understanding of the complex relationships between these objects in both space and time.

23.2 Visual Representation

The 3D plot below provides a visual representation of this particle cloud concept. The current positions of the Messier objects are shown in purple, while their past positions are shown in cyan. This representation aims to offer a more dynamic and full view of the topological space.



Particle Cloud Description of Local Vision